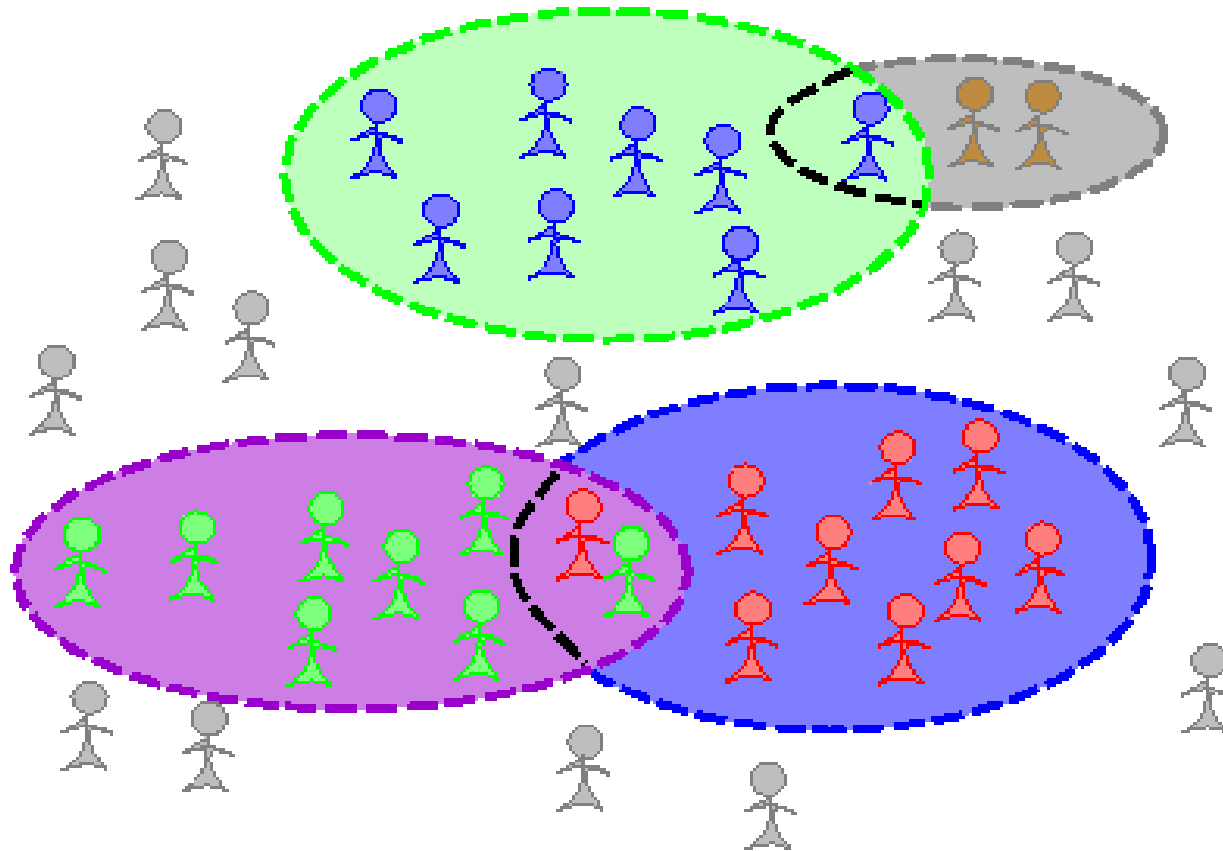
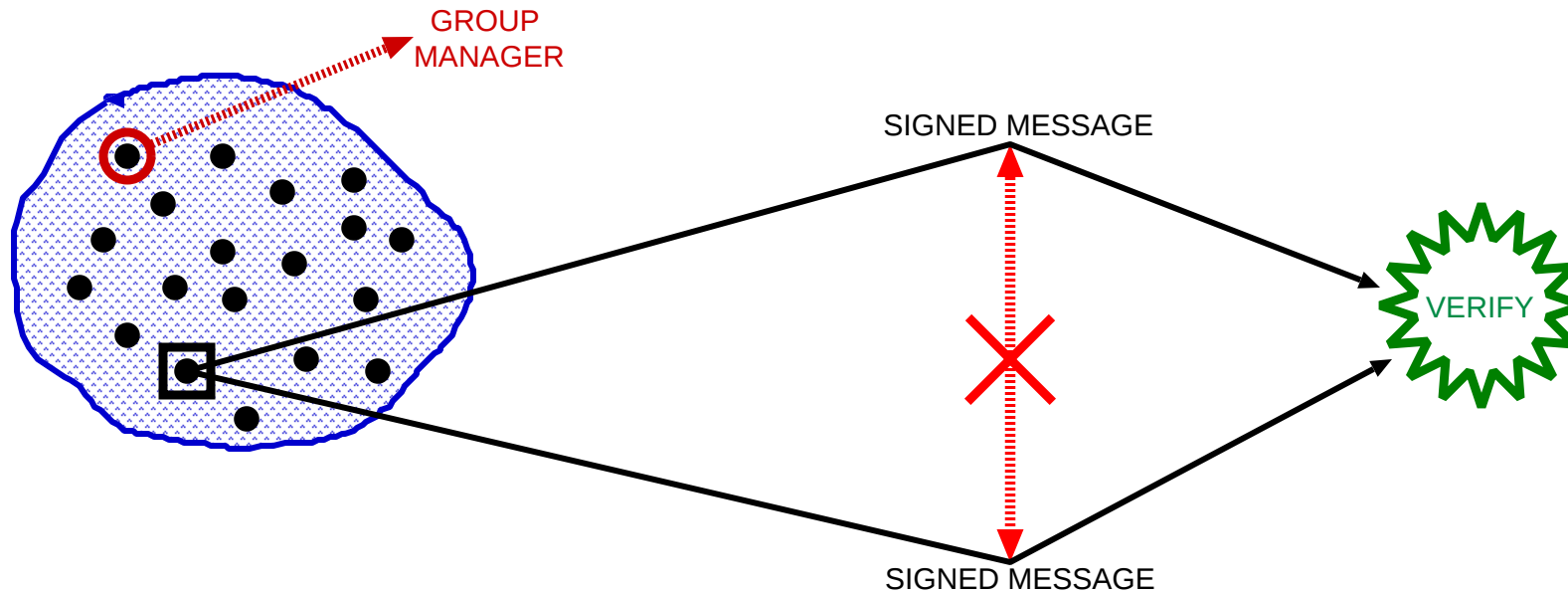


Efficient Group Signature Schemes



Giuseppe Ateniese and Gene Tsudik
USC Information Sciences Institute
ateniese@ISI.EDU
gts@ISI.EDU

Group Signature



- Unforgeability, Anonymity, Unlinkability, Exculpability, Traceability
- Efficiency and Size (group PK, signature)

Basic Phases

- **SETUP:** $-(n, v, a, Y, Z)-$

-> $n = pq, p=2p'+1 \quad q=2q'+1;$

-> $v, \gcd(v, (p-1)(q-1))=1;$

-> a , of large mult. order mod both $p, q;$

-> $Y, a^{-y};$

-> $Z, a^z;$

- **JOIN:**

-> send $a^x, v < x \quad \gcd(v, x)=1;$

-> group certificate: $A=a^{[(x+y)/v]};$

-> store significant information in the membership table;

Basic Phases

- SIGN:

$$\rightarrow T1 = A a^r$$

$$\rightarrow T2 = A^{-1} (Z a^{-1})^r$$

$\rightarrow$ Construct:

$$SKLOG1 = SKLOG(m, a^{(x+rv)}, a);$$

$$SKLOG2 = SKLOG(m, a^{(zr)}, a^z);$$

$\rightarrow$ Send $\{T1, T2, SKLOG1, SKLOG2\};$

- VERIFY:

$$\rightarrow W1 = (T1^v) Y (= a^{(x+rv)});$$

$$\rightarrow W2 = (T1 T2) (= a^{(rz)} = Z^r);$$

$\rightarrow$ check SKLOG1 and SKLOG2 with W1, W2;

- OPEN:

$$\rightarrow ID = (T1)^{(z-1)} T2^{-1} = A^z;$$

Coalitions and Previous Works

- C./S. crypto'97:

-> group certificate: $A=(a^x + 1)^d$, $d=1/e$;

- Some attacks: $(a^x+1) = a^x(1+a^{-x})$

-> if $x = ke$, from $a^k (1+a^{-x})^d$
 $\implies (a^{-x} + 1)^d$;

-> User 1 registers $(a^x + 1)^d$

User 2 registers $(a^{-x} + 1)^d$
 $\implies a^{(xd)}$

User 3 registers $(a^{(-cx)} + 1)^d$
 $\implies (a^{(cx)} + 1)^d$

-> $a^{(C_1 X_1 d)}, \dots, a^{(C_n X_n d)}$
 $\implies (a^{(C_1 X_1 + \dots + C_n X_n)} + 1)^d$

Our Approach and On-going Work

- Cross-check by several group certificates
- How many ?
- Pooling shares is only a specific form of coalition